

Minimisation of the Dirichlet Energy amongst a class of constrained maps

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Energy Functionals and Jacobian Constraints

We consider minimising the **Dirichlet energy**

$$\mathbb{D}(v) = \int_B |\nabla v|^2 \, dx$$